

Sec 5.1.1 Systems of Equations (2 variables)

Determine if (-3,5) is a solution to

$$\begin{aligned} 9x + 7y &= 8 \\ 8x - 9y &= -69 \end{aligned}$$

$$\begin{aligned} 9(-3) + 7(5) &= 8 ? \\ -27 + 35 &= 8 ? \quad \text{yes} \end{aligned}$$

$$\begin{aligned} 8(-3) - 9(5) &= -69 ? \\ -24 - 45 &= -69 \end{aligned}$$

Solve using the substitution method-

$$\begin{aligned}x &= 3y + 7 \\x &= 2y - 1\end{aligned}$$

$$\begin{aligned}2x - 3y &= -13 \\y &= 2x + 7\end{aligned}$$

$$3y + 7 = 2y - 1$$

$$y = -8$$

$$\begin{aligned}x &= 3(-8) + 7 \\&= -24 + 7 \\&= -17\end{aligned}$$

Solve using the a combination-
(aka, addition, subtraction,
multiplication)

$$\begin{array}{r} -9x - 6y = 18 \\ \underline{-9x + y = 18} \\ -7y = 0 \\ y = 0 \\ -9x = +18 \\ x = -2 \\ (-2, 0) \end{array}$$

Subtract

$$\begin{array}{r} -x + 8y = 14 \\ + (x + 3y = -3) \\ \hline 11y = 11 \end{array}$$

add

$$\begin{array}{r} 11y = 11 \\ y = 1 \\ -x + 8 = 14 \\ -x = 6 \quad x = -6 \end{array}$$

$$(-6, 1)$$

Solve using the a combination-

$$\begin{array}{r} (3x - 7y = 13) \times 2 \rightarrow \\ 6x - 14y = 26 \\ 6x + 5y = 7 \\ \hline -19y = 19 \\ y = -1 \\ (25) \end{array}$$
$$\begin{array}{l} 6x - 5 = 7 \\ 6x = 12 \\ x = 2 \end{array}$$

Determine the point of intersection-

$$6\left(\frac{x}{6} - \frac{y}{2} = \frac{1}{3}\right) \rightarrow x - 3y = 2$$
$$x + 2y = -3 \quad - (x + 2y = -3)$$

$$-5y = 5$$
$$y = -1$$

back sub...

You're solving a system...
....all the variables cancel and
a true statement
(i.e. $3 = 3$) remains...

infinitely many

You're solving a system... solutions
....all the variables cancel and
a false statement
(i.e. $0 = 2$) remains...



Suggested Practice

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1,5,9,15,17

19,23,29,

31,33

Solutions-

1. solution
5. $(1,3)$
9. $(-22,-5)$
15. $(5,4)$
17. $(7,3)$

19. $(2,-1)$
23. $(-4,3)$
29. $(7/25,-1/25)$
31. no solution
33. infinitely many
solutions

