

Sec 2.2.3 Piece-wise Functions



*a function defined by more than one equation
over a specified domain*

-Example-

"usage" rates....if you use less than a certain
amount you're charged at one rate, more than
a certain amount, charged a different rate

purchasing...if purchasing a small
number of something charged one price
but if purchasing a larger number
charged a different price...

Given: $f(x) = \begin{cases} 3x+5, & \text{if } x < 0 \\ 4x+7, & \text{if } \underline{x \geq 0} \end{cases}$

Determine
 $f(-2)$

use $3x+5$ $x < 0$
 $= 3(-2) + 5$
 $= -1$

$f(0)$ x
 $4(0) + 7$
 $= 7$

$f(3)$ $x \geq 0$
use $4x+7$
 $4(3) + 7$
 $= 19$

$$\text{Given: } f(x) = \begin{cases} \frac{x^2 - 16}{x - 4}, & \text{if } x \neq 4 \\ 8, & \text{if } x = 4 \end{cases}$$

Determine $f(0)$

$$\frac{0^2 - 16}{0 - 4}$$

$$= 4$$

$x \neq 4$

$f(4)$

$x = 4$

$$f(4) = 8$$

Determine

$$g(x) = \begin{cases} 3, & x \leq -1 \\ 2x - 3, & -1 < x \leq 3 \\ \frac{4}{x}, & x > 3 \end{cases}$$

$g(-5) = 3$

$g(-1) = 3$

$g(0) = 2(0) - 3 = -3$

$g(3) = 2(3) - 3 = 3$

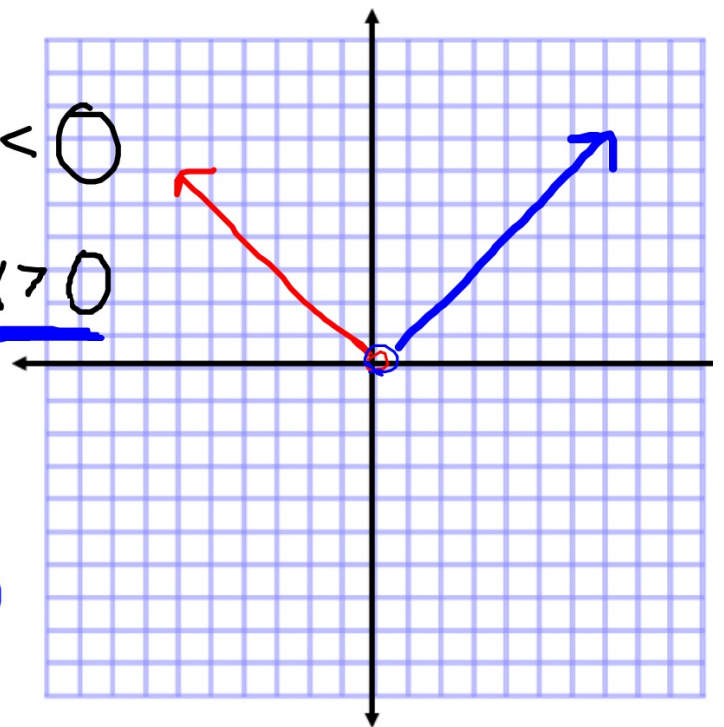
$g(5) = \frac{4}{5}$

Graph -

$$f(x) = \begin{cases} -x & \text{if } x < 0 \\ x & \text{if } \underline{x > 0} \end{cases}$$

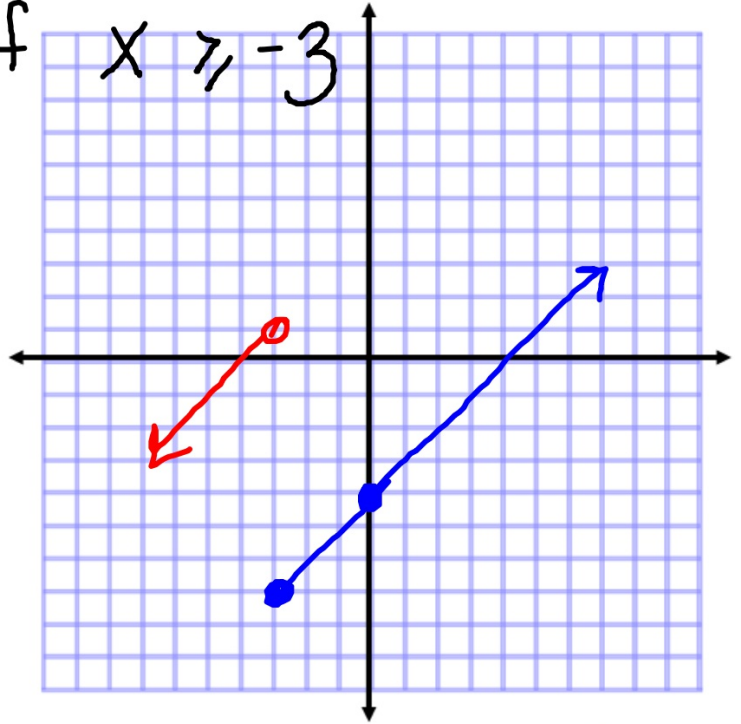
$$\begin{aligned} y &= -x \\ x &< 0 \end{aligned}$$

$$\begin{aligned} y &= x \\ x &> 0 \end{aligned}$$



$$f(x) = \begin{cases} \bullet x+4, & \text{if } x < -3 \\ \bullet x-4, & \text{if } x \geq -3 \end{cases}$$

BTW
 $f(-3) = 7$



Suggested Practice
Sec 2.2
pages 240-241
39,41,42
44,45,47,49,51,53,54



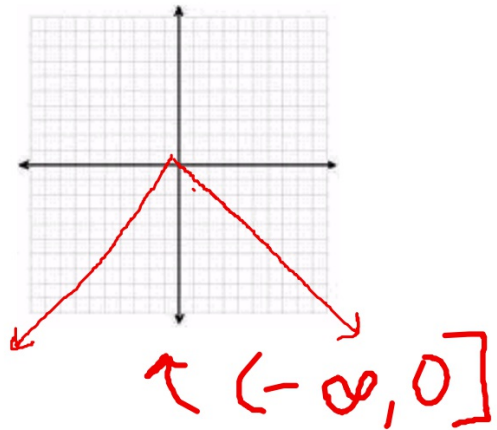
39. a. 3
b. 3
c. 0

41. a. 8 c. 6
b. 3

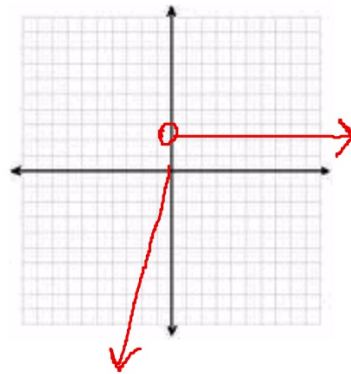
42. a. 12
b. 5
c. 10

$(-\infty, 0] \cup [2, \infty)$

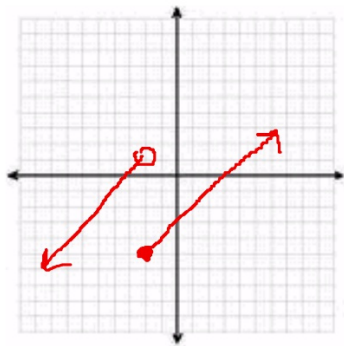
44.



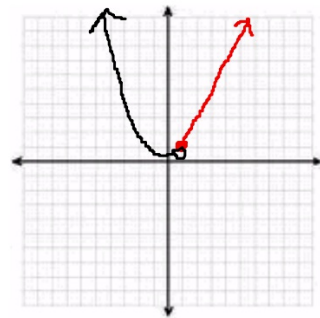
45.



47.

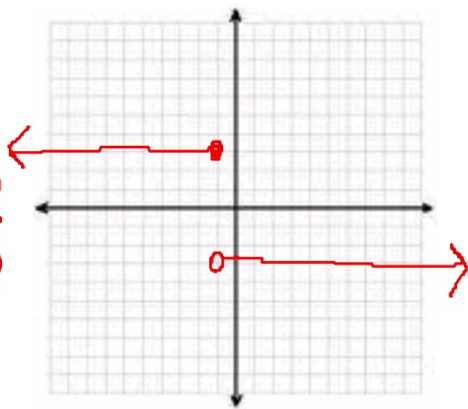


51.

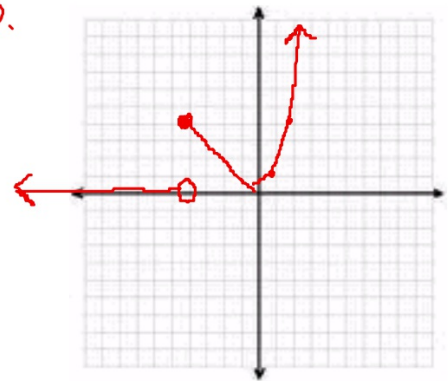


49.

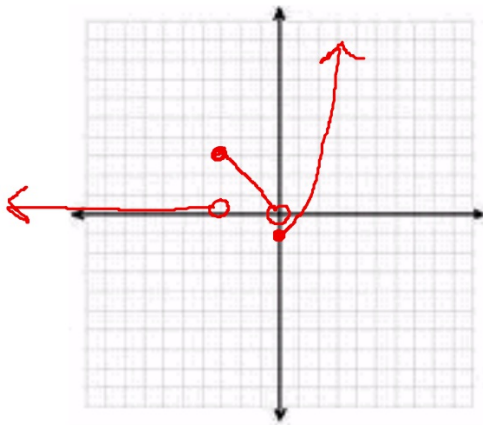
$$r: \{\pm 3\}$$



53.



54.



$$r: [-1, \infty)$$

$$f(-3) = 3$$

$$f(0) = -1$$

