

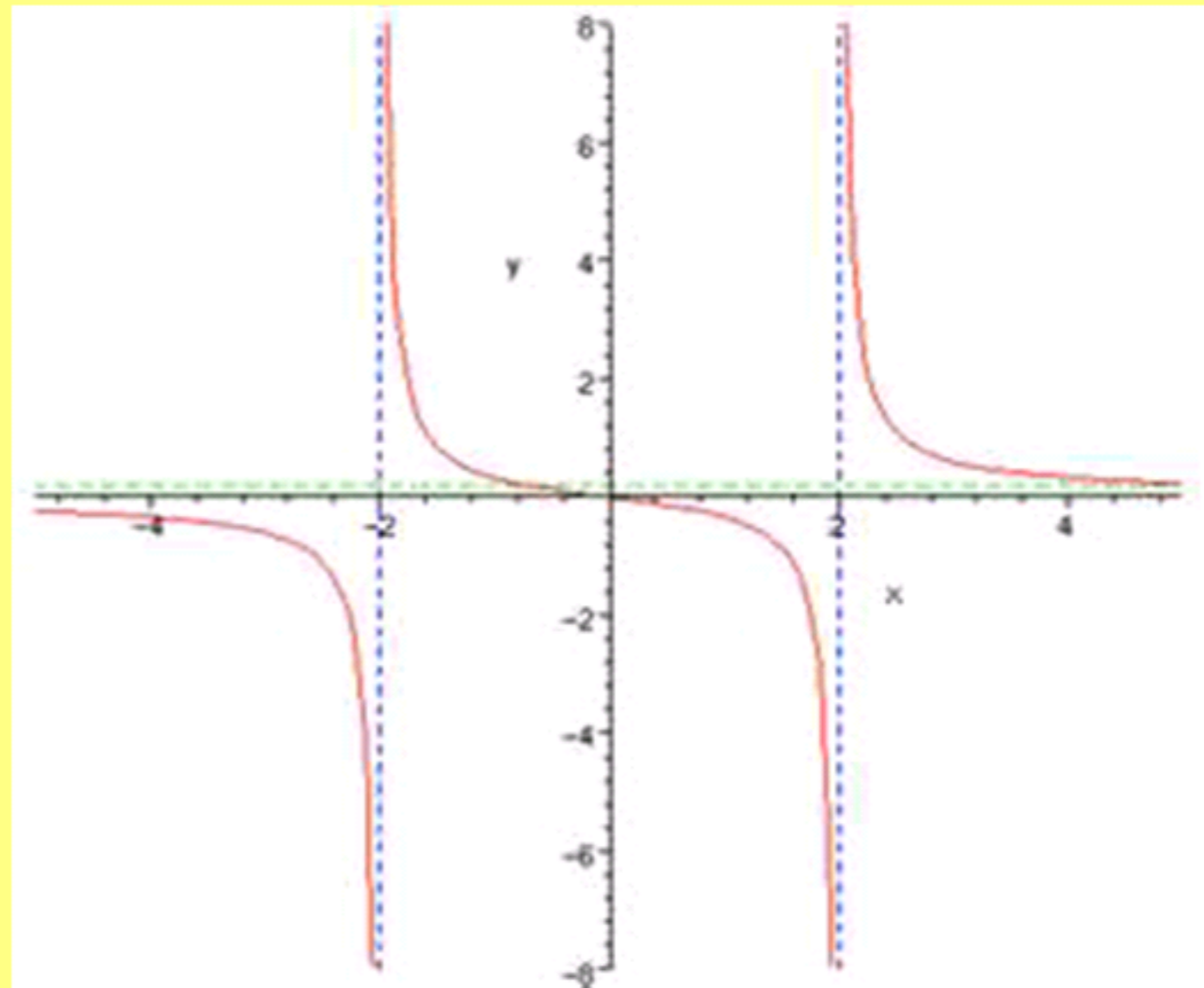
Sec 3.5

Finding vertical and horizontal asymptotes

Asymptotes act like boundaries for a graph. On both sides, the graph will approach either negative, or positive, infinity.

Yesterday, we described asymptotic behavior and end behavior.

Today...finding the asymptotes that cause it.



Three types of asymptotes occur:

- ① Vertical
- ② Horizontal
- ③ Slant/oblique

Well work with only vertical & horizontal in one lesson; slant in another.

Finding vertical

Simple! Set denominator equal to zero and solve.

Example-

$$f(x) = \frac{x}{x^2 - 9}$$

VA's

$$x = \pm 3$$

$$f(x) = \frac{x+4}{x^2 - 16}$$

$$\frac{\cancel{x+4}}{(\cancel{x+4})(x-4)}$$

VA @ $x = 4$
hole @ $x = -4$



$$f(x) = \frac{x+4}{x^2 + 16}$$

$$x^2 + 16 = 0$$
$$\sqrt{x^2} = \sqrt{-16}$$

no
VA's

Finding horizontal

We will compare the degree of the numerator vs. denominator, where " n " is the degree of the numerator and " m " is the degree of the denominator.

- If $n < m$ there is a horizontal asymptote @ $y = 0$
- If $n = m$, there is a horizontal asymptote at the ratio of the leading coefficients
 - If $n > m$ there is no horizontal asymptote
(this is when slant asymptotes will occur, however)

$n = m$


$n < m$

$n > m$

horizontal at ratio

horizontal at $y = 0$

none


$$\frac{6-4x}{5+2x}$$

HA @ $y = -2$

$$\frac{4x+3}{x^3-8}$$

HA @ $y = 0$

$$\frac{6x^3+2}{x^2}$$

no HA

(later: slant)



Suggested Practice
Sec 3.5 page 406/407
21-44 odds

*find asymptotes only...no graphing today



21. VA @ $x = -4$

23. VA @ $x = -4$
 $x = 0$

25. VA @ $x = -4$
hole @ $x = 0$

27. none

29. hole @ $x = 3$

31. VA @ $x = -3$
hole @ $x = 3$

33. VA @ $x = 3$
hole @ $x = -7$

35. hole @ $x = -7$

37. $y = 0$

39. $y = 4$

41. no HA

43. $y = -2/3$